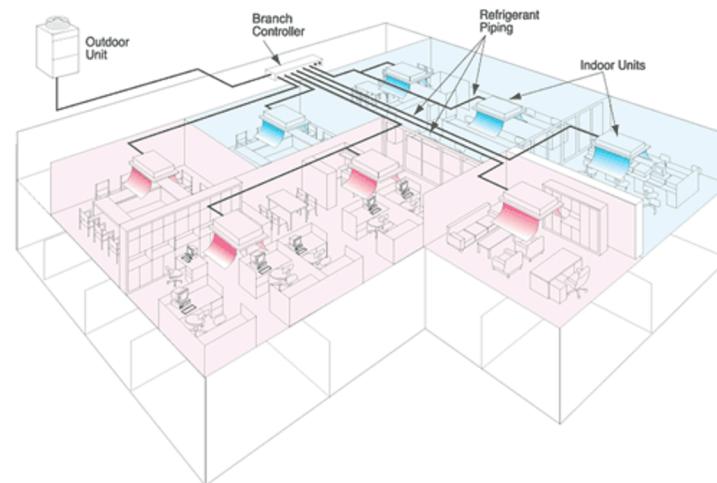


**MITSUBISHI ELECTRIC RESEARCH LABORATORIES**  
Cambridge, Massachusetts

# ANP-BBO: Attentive Neural Processes and Batch Bayesian Optimization for Scalable Calibration of Physics-Informed Digital Twins



Ankush Chakrabarty  
Gordon Wichern  
Christopher Laughman

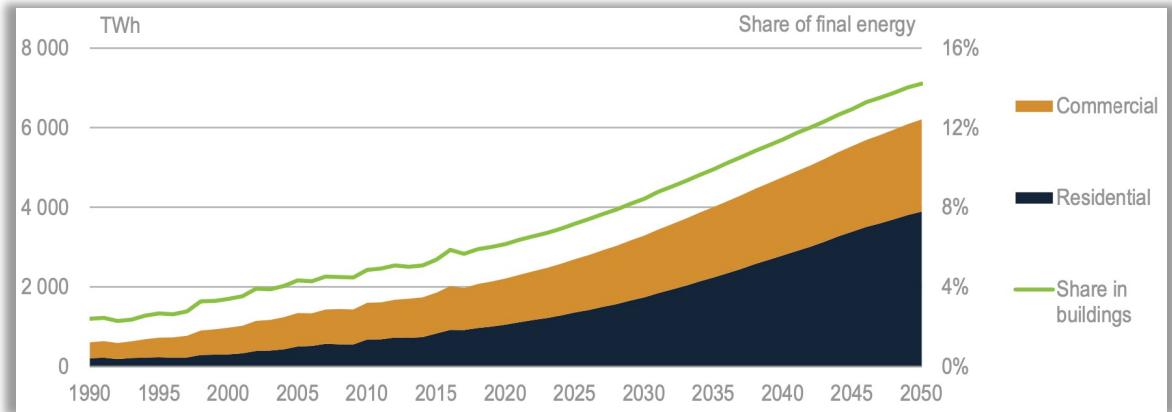
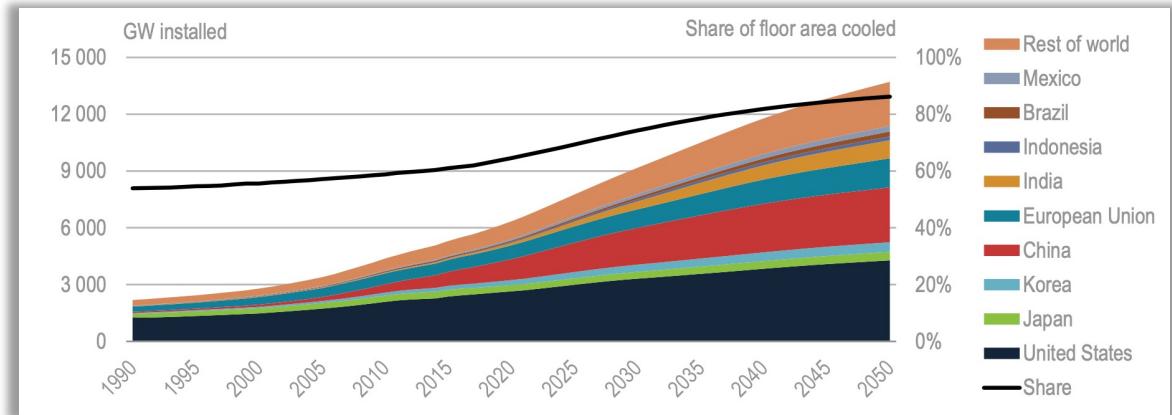
✉ [achakrabarty@ieee.org](mailto:achakrabarty@ieee.org)

Due to climate change, global trends project<sup>[1]</sup>

- space cooling demand will rise **from 60% to >85%**
- energy needs for space cooling will **>3x**

between 2016 and 2050

## Digital Twins and Climate Change



[1] International Energy Agency, *The Future Of Cooling*, 2018.

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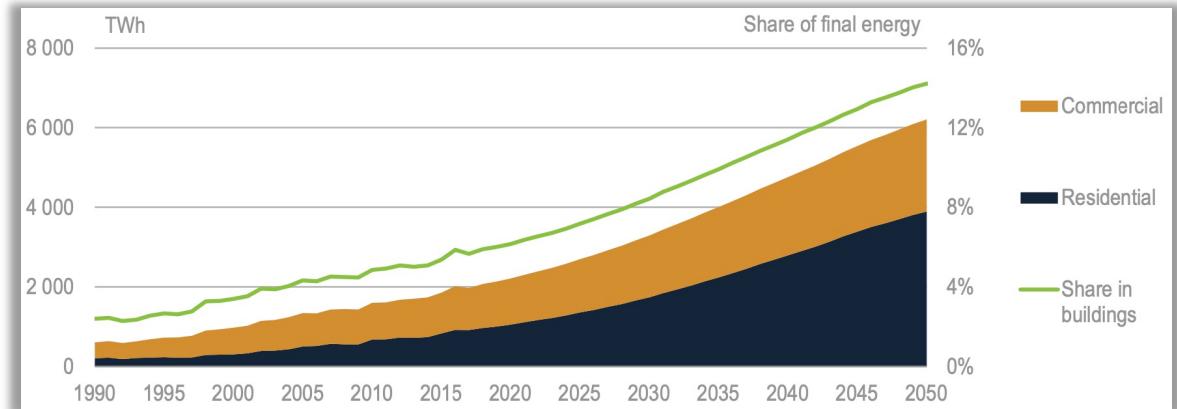
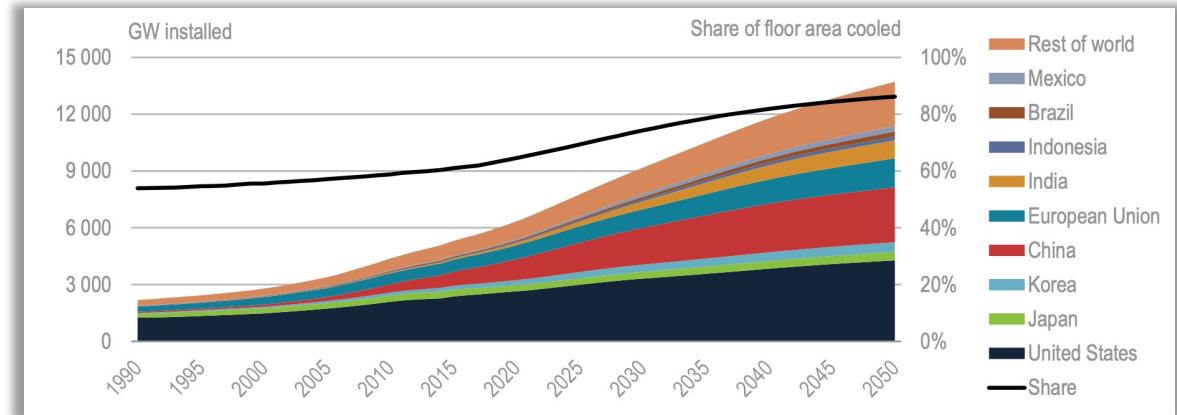
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- ML has been identified as enabling technology for building optimization<sup>[2]</sup>
- Many field experiments for data is impractical

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[1] International Energy Agency, *The Future Of Cooling*, 2018.

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**Digital twins** (DTs) enable safe experiments via simulation, but they **need to be calibrated to accurately reflect truth**

## Digital Twins and Climate Change



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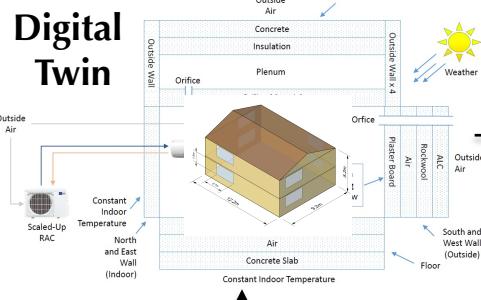
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Building System + HVAC



Measured data

$y_{0:T}^*$

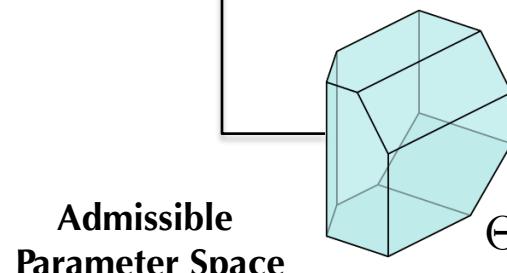


Model outputs  
 $y_{0:T} = \mathcal{M}_T(\theta)$

$$J(y_{0:T}^*, \mathcal{M}_T(\theta_t))$$

Calibration Cost

Simulate model



# Calibration of Physics-Informed Digital Twins

## Examples of $\theta$

Building: airflow coefficients, material properties

HVAC: heat transfer coefficients, refrigerant properties

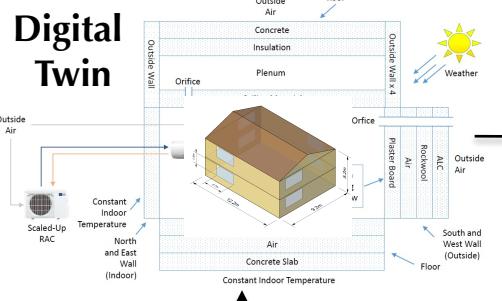
$$\theta^* = \arg \min_{\Theta} J$$

## Building System + HVAC



Measured data

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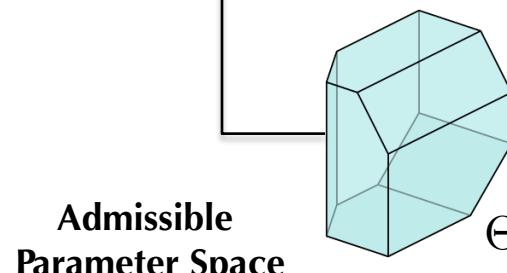


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# Calibration of Physics-Informed Digital Twins

## Examples of $\theta$

*Building:* airflow coefficients, material properties

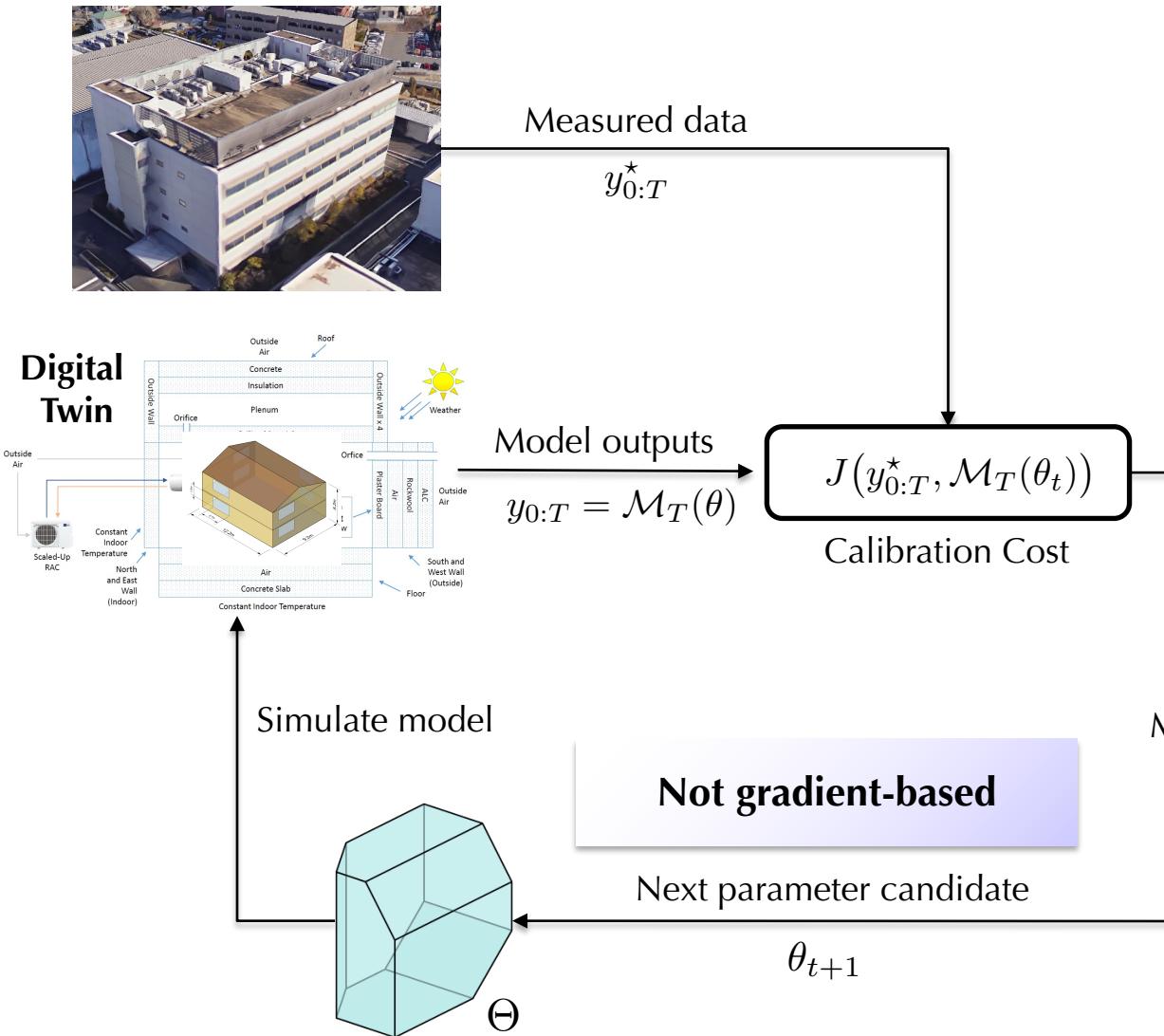
*HVAC:* heat transfer coefficients, refrigerant properties

$$\theta^* = \arg \min_{\Theta} J$$

## Objective:

Use simulations to obtain parameters  $\theta^*$  that minimize the calibration cost

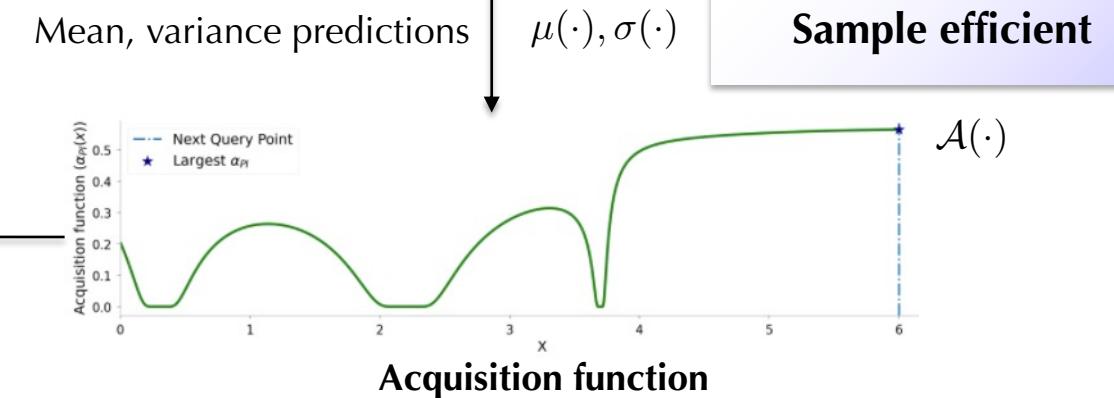
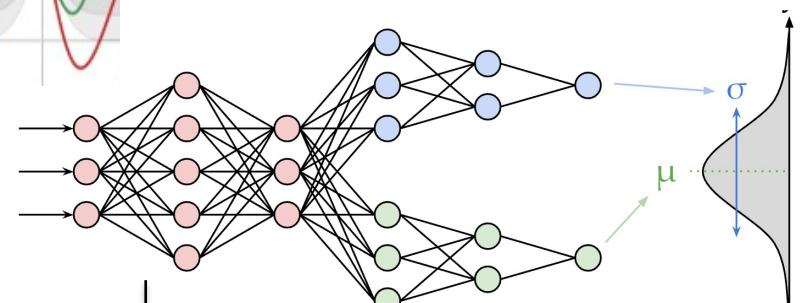
Building System + HVAC



# Calibration of Physics-Informed Digital Twins (via Bayesian Optimization)

Can scale up

Approximate Calibration Cost with  
Probabilistic Learners



## ANP-BBO: Why not GPs?

### GP-BO:

- ✗ Inference is expensive
- ✗ Limited to Gaussian distributions
- ✗ Simulations/cost evaluation not parallelizable

### Proposed ANP-BBO:

- ✓ Inference is cheap<sup>[1]</sup>
- ✓ Wide range of distributions<sup>[2]</sup>
- ✓ Simulations/cost evaluation can be parallelized

[1] Kim et al. *Attentive Neural Processes*. <https://arxiv.org/pdf/1901.05761.pdf>

[2] Garnelo et al. *Neural processes*. arXiv preprint arXiv:1807.01622.

ANP-BBO: Attentive Neural Processes-Batch Bayesian Optimization

## ANP-BBO: Algorithm

GP-BO:

- ✗ Inference is expensive
- ✗ Limited to Gaussian distributions
- ✗ Simulations/cost evaluation not parallelizable

i. Current dataset after  $t$  iterations  $D^t = \{(\theta, J)\}_0^{N_0+tN}$

ii. Train ANP by maximizing ELBO with  $N$  new data points

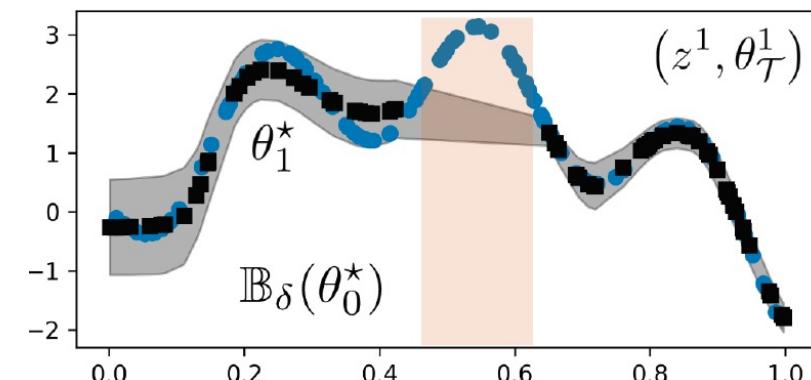
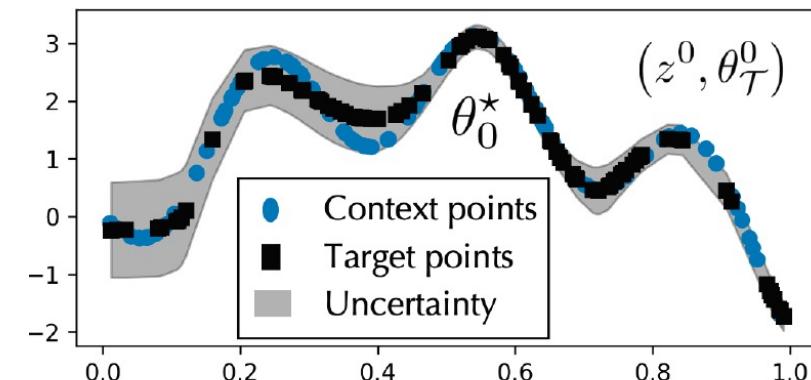
iii. Select batch of  $N$  candidates during inference

- Sample a latent,  $z$  (*Cheap inference*)
- Perform target set penalization (*Wide range*)

iv. (*Parallelizable*) Simulate to evaluate cost (via digital twin)

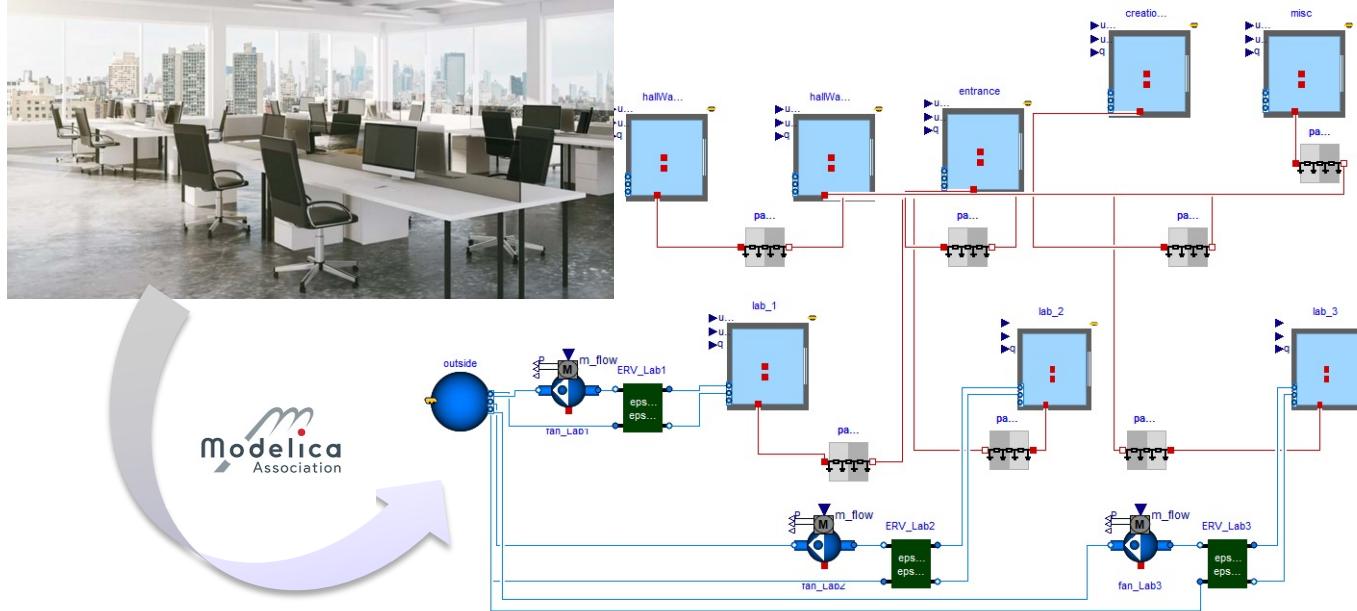
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# ANP-BBO: Calibration Results

## Digital Twin of 1 Floor of Commercial Building in Tokyo, JP



### Setup:

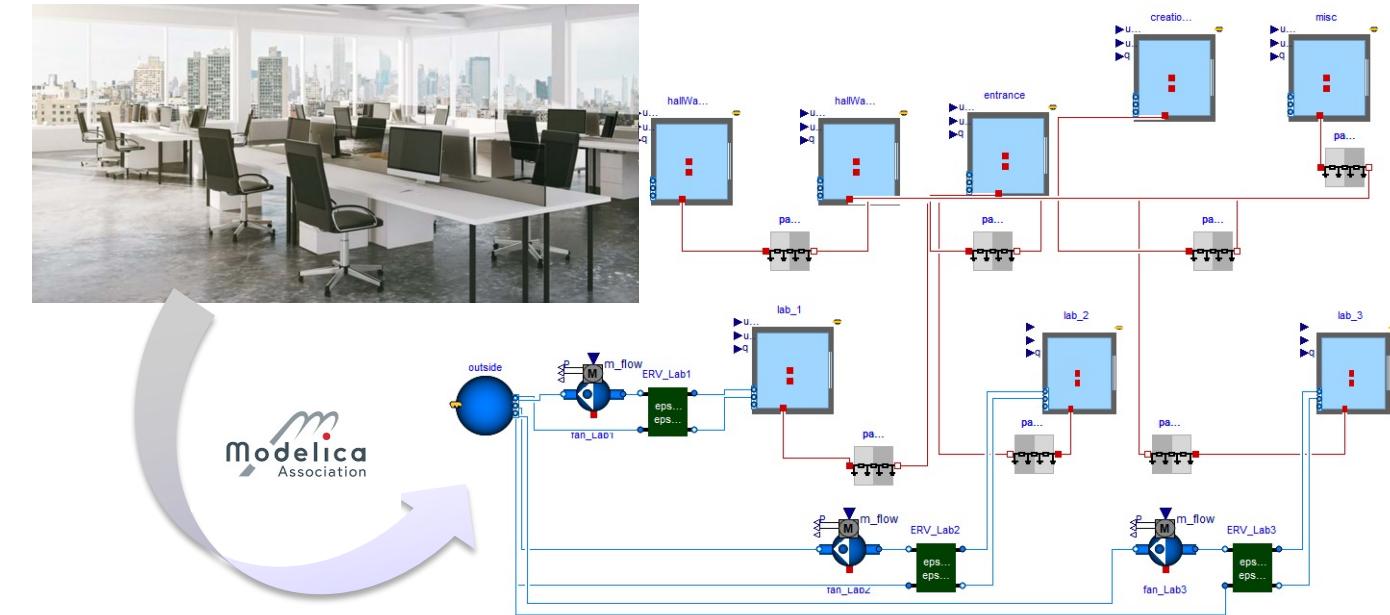
- 12 parameters to be calibrated
- 5 days of measured temp. and RH data, noisy, quantized
- 2 days for calibration, 3 days for testing

[1] ASHRAE, *Guideline 14-2014, measurement of energy, demand, and water savings*. 2014.

R-x: Room number x,  $x \in \{1,2,3\}$

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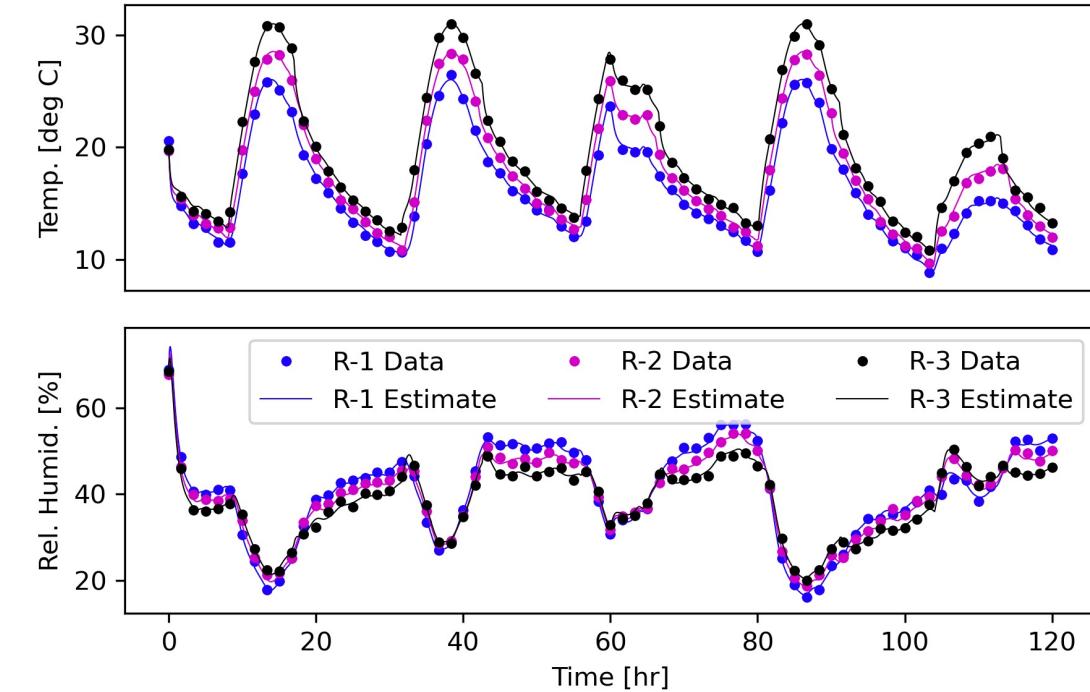


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[1] ASHRAE, *Guideline 14-2014, measurement of energy, demand, and water savings*. 2014.

## Measured and simulated outputs

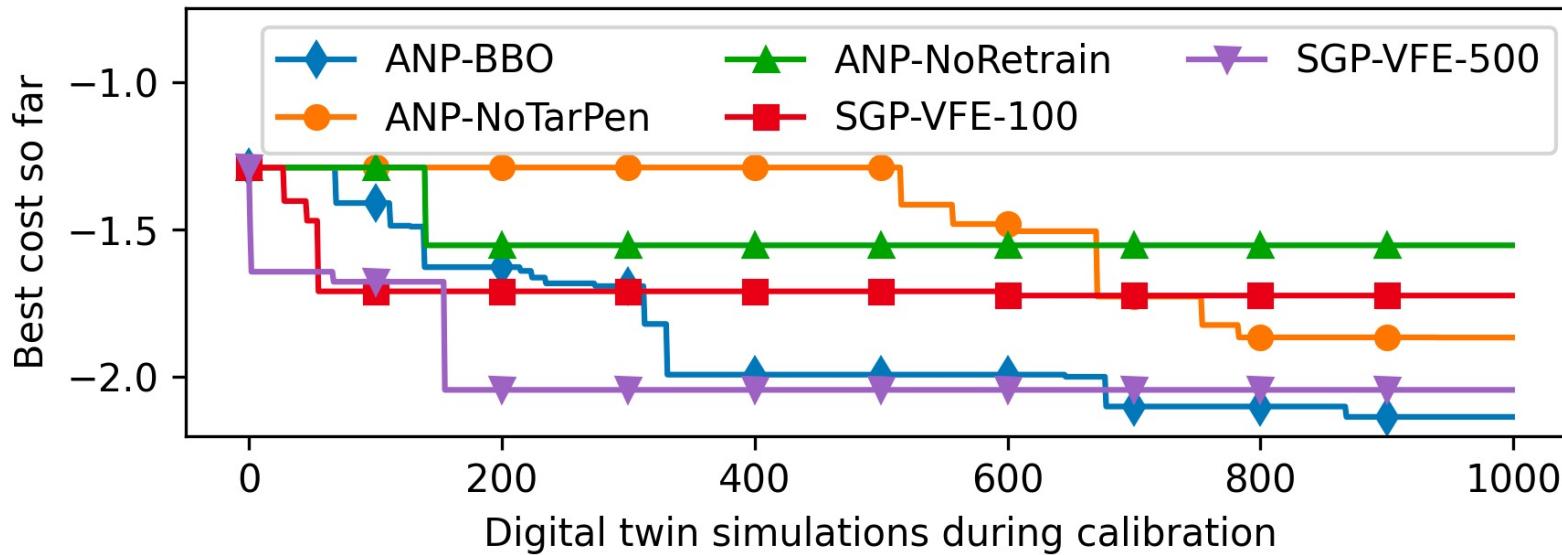


Outputs coefficient of variation of RMSE is  $<1\%$ , well within the ASHRAE guidelines  $<15\%$  <sup>[1]</sup>

R-x: Room number x,  $x \in \{1,2,3\}$

## ANP-BBO: Ablation Studies

1. ANP-BBO: Proposed algorithm
2. ANP-NoTarPen: Switch off target set penalization
3. ANP-NoRetrain: Train ANP once with initial data, no further retraining
4. SGP-VFE-100/500: Use sparse Gaussian processes<sup>[1]</sup> as learner, with 100 or 500 inducing points



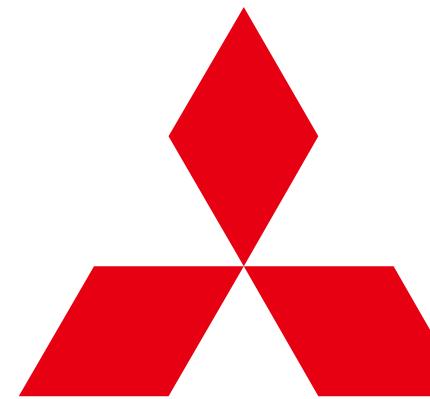
ANP-NoTarPen: Shows target penalization helps more than only latent sampling

ANP-NoRetrain: Lack of retraining with limited initial data does poorly

SGP-VFE: Good early, but gets stuck due to worsening approximations at scale

ANP-BBO: outperforms the others after 700 iters due to diverse and good candidates

[1] Titsias. Variational learning of inducing variables in sparse Gaussian processes. AISTATS, 2009.



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