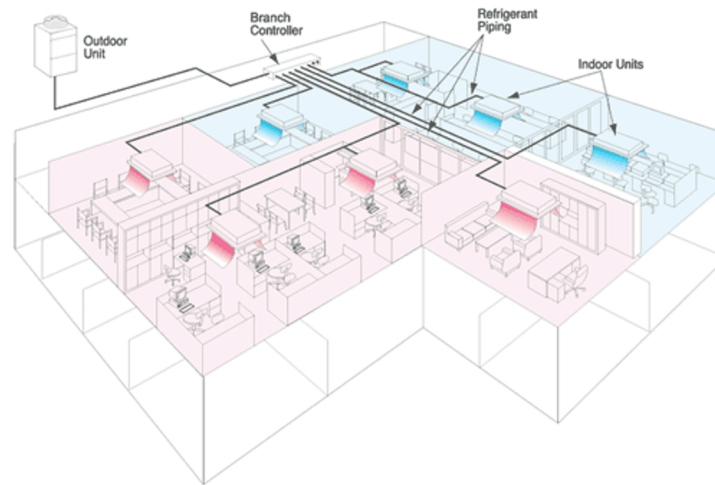
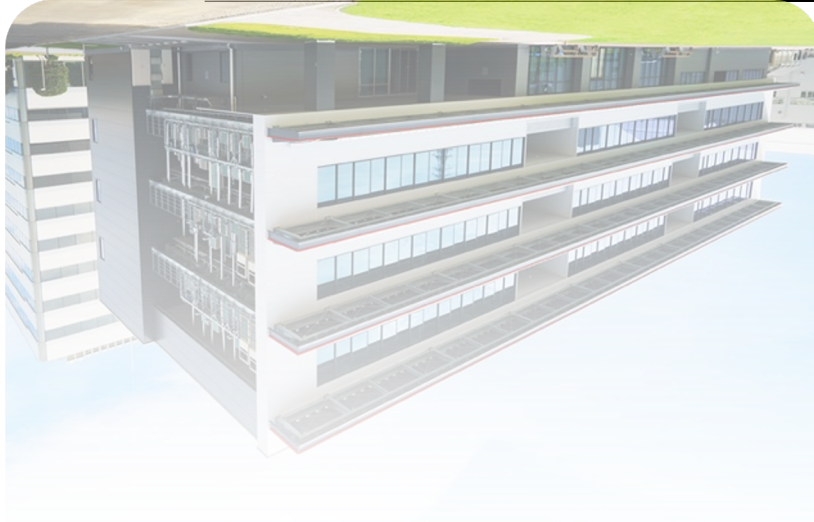




MITSUBISHI ELECTRIC RESEARCH LABORATORIES
Cambridge, Massachusetts

ANP-BBO: Attentive Neural Processes and Batch Bayesian Optimization for Scalable Calibration of Physics-Informed Digital Twins



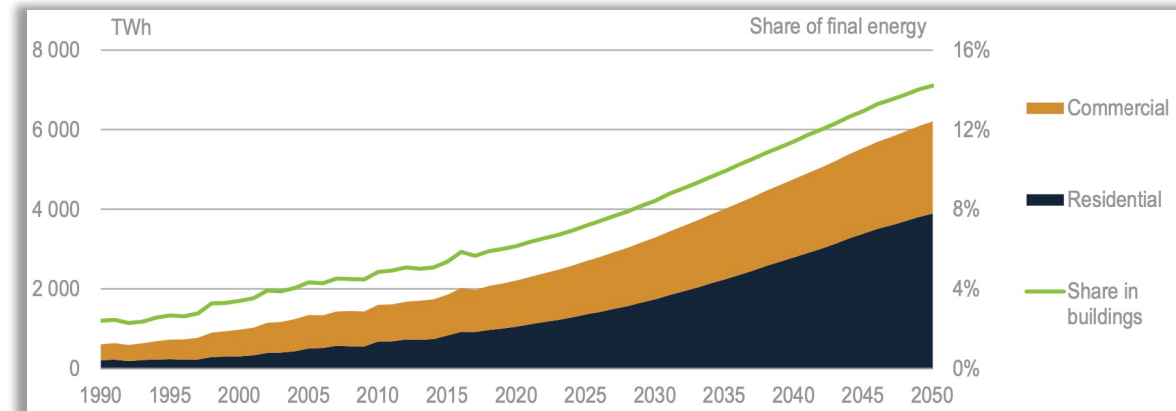
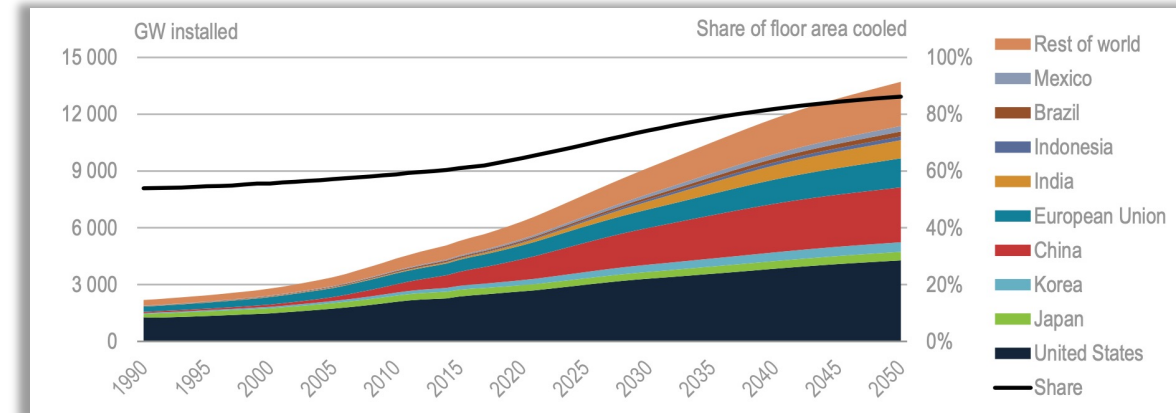
Ankush Chakrabarty
Gordon Wichern
Christopher Laughman

✉ achakrabarty@ieee.org

Digital Twins and Climate Change

Due to climate change, global trends project^[1]

- space cooling demand will rise **from 60% to >85%**
- energy needs for space cooling will **>3x** between 2016 and 2050



[1] International Energy Agency, *The Future Of Cooling*, 2018.

Digital Twins and Climate Change

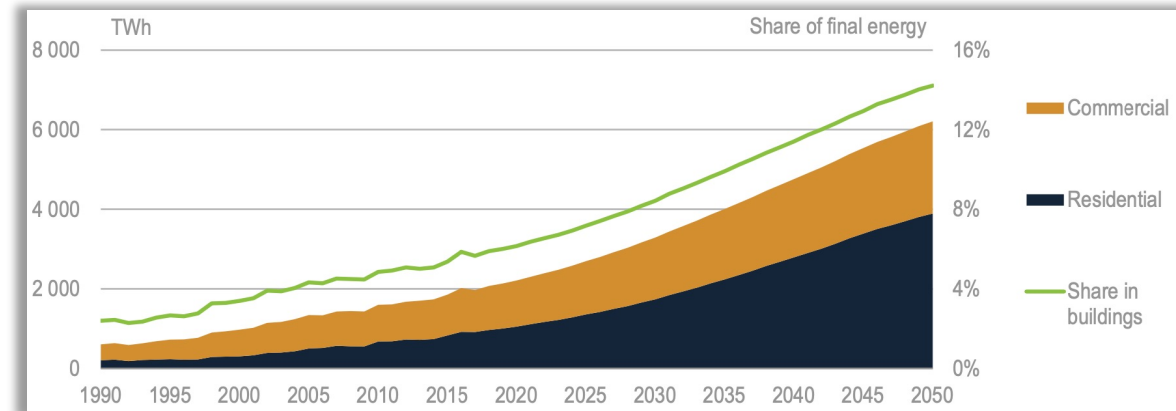
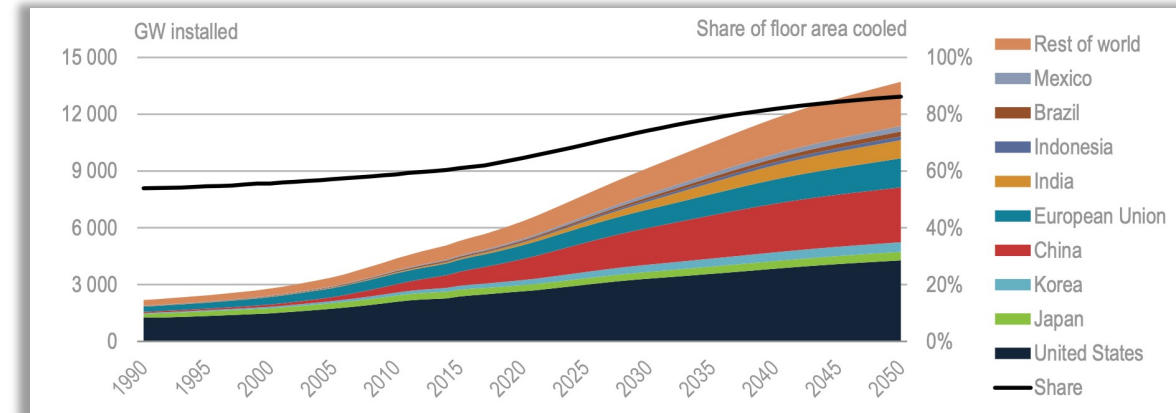
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- Many field experiments for data is impractical



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[2] Rolnick et al., *Tackling Climate Change with Machine Learning*, arXiv:1906.05433, 2019.

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Digital twins (DTs) enable safe experiments via simulation, but they **need to be calibrated to accurately reflect truth**



[1] International Energy Agency, *The Future Of Cooling*, 2018.

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Building System + HVAC



Measured data

$$y_{0:T}^*$$

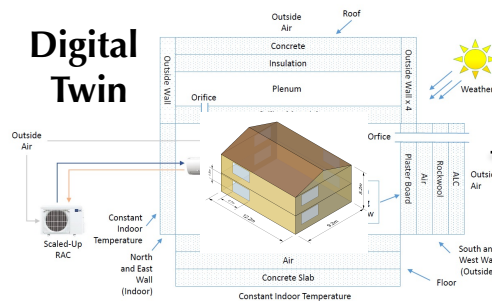
Calibration of Physics-Informed Digital Twins

Examples of θ

Building: airflow coefficients, material properties

HVAC: heat transfer coefficients, refrigerant properties

Digital Twin



Model outputs

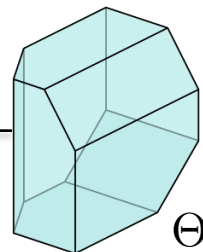
$$y_{0:T} = \mathcal{M}_T(\theta)$$

$$J(y_{0:T}^*, \mathcal{M}_T(\theta_t))$$

Calibration Cost

$$\theta^* = \arg \min_{\Theta} J$$

Simulate model



Θ

**Admissible
Parameter Space**

Building System + HVAC



Measured data

$$y_{0:T}^*$$

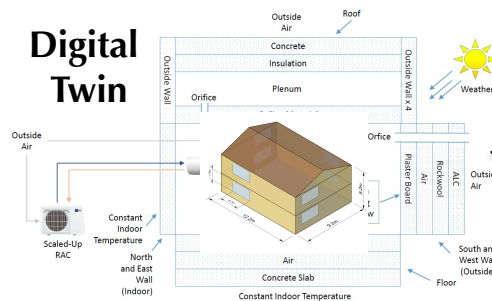
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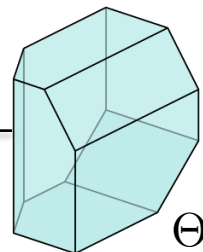
$$\theta^* = \arg \min_{\Theta} J$$

Objective:

Use simulations to obtain parameters θ^* that minimize the calibration cost

Simulate model

**Admissible
Parameter Space**



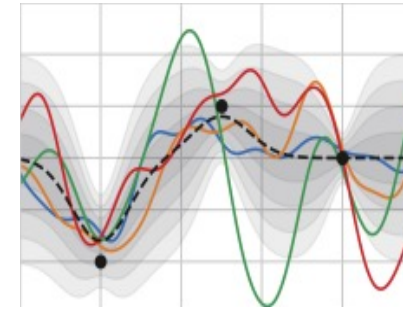
Building System + HVAC



Measured data

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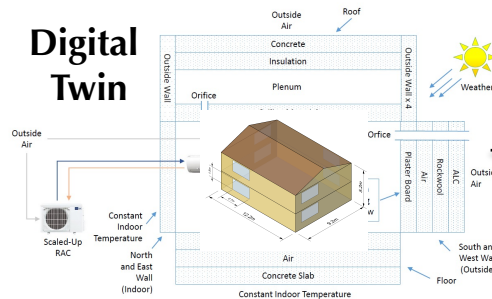
Calibration of Physics-Informed Digital Twins (via Bayesian Optimization)



Can scale up

Approximate Calibration Cost with Probabilistic Learners

Digital Twin

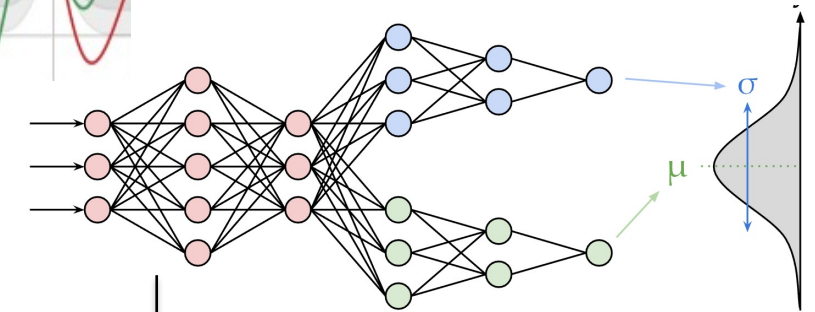


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Calibration Cost



Mean, variance predictions

$$\mu(\cdot), \sigma(\cdot)$$

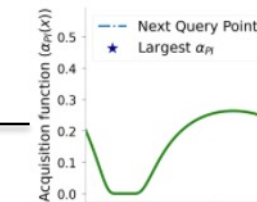
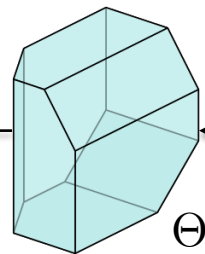
Sample efficient

Not gradient-based

Next parameter candidate

$$\theta_{t+1}$$

Simulate model



Acquisition function

ANP-BBO: Why not GPs?

GP-BO:

- X Inference is expensive
- X Limited to Gaussian distributions
- X Simulations/cost evaluation not parallelizable

Proposed ANP-BBO:

- ✓ Inference is cheap^[1]
- ✓ Wide range of distributions^[2]
- ✓ Simulations/cost evaluation can be parallelized

[1] Kim et al. *Attentive Neural Processes*. <https://arxiv.org/pdf/1901.05761.pdf>

[2] Garnelo et al. *Neural processes*. arXiv preprint arXiv:1807.01622.

ANP-BBO: Algorithm

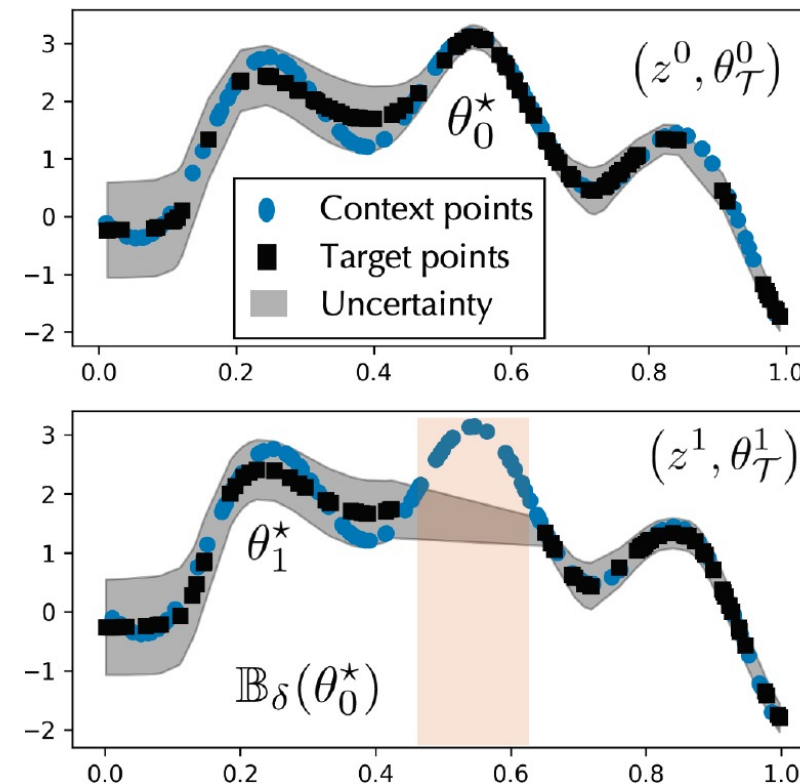
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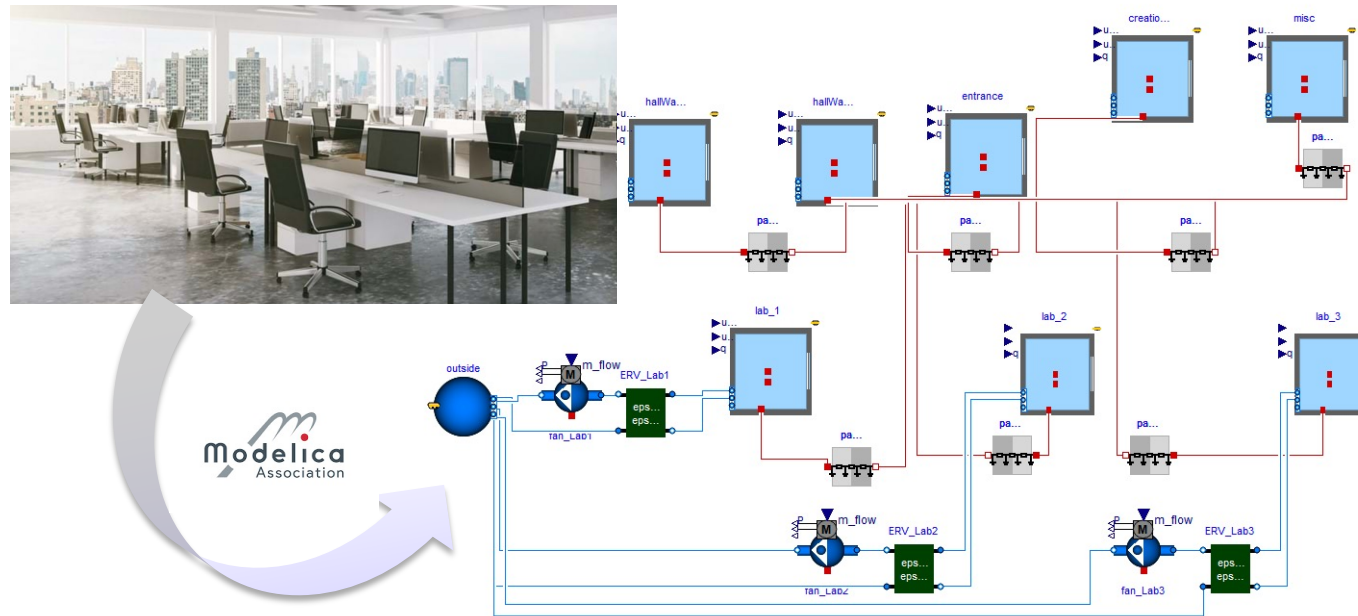
- ✓ Inference is cheap
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- i. Current dataset after t iterations $D^t = \{(\theta, J)\}_0^{N_0+tN}$
- ii. Train ANP by maximizing ELBO with N new data points
- iii. Select batch of N candidates during inference
 - Sample a latent, z (*Cheap inference*)
 - Perform target set penalization (*Wide range*)
- iv. (*Parallelizable*) Simulate to evaluate cost (via digital twin)



ANP-BBO: Calibration Results

Digital Twin of 1 Floor of Commercial Building in Tokyo, JP



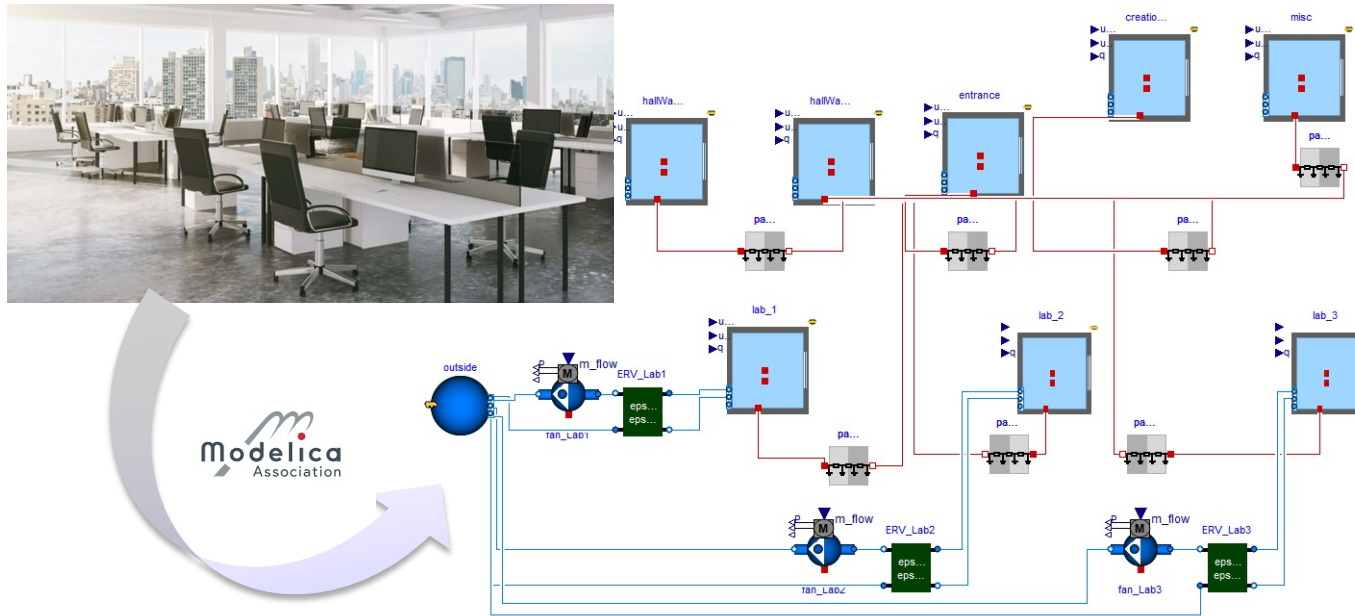
Setup:

- 12 parameters to be calibrated
- 5 days of measured temp. and RH data, noisy, quantized
- 2 days for calibration, 3 days for testing

[1] ASHRAE, *Guideline 14-2014, measurement of energy, demand, and water savings*. 2014.

R-x: Room number x, $x \in \{1,2,3\}$

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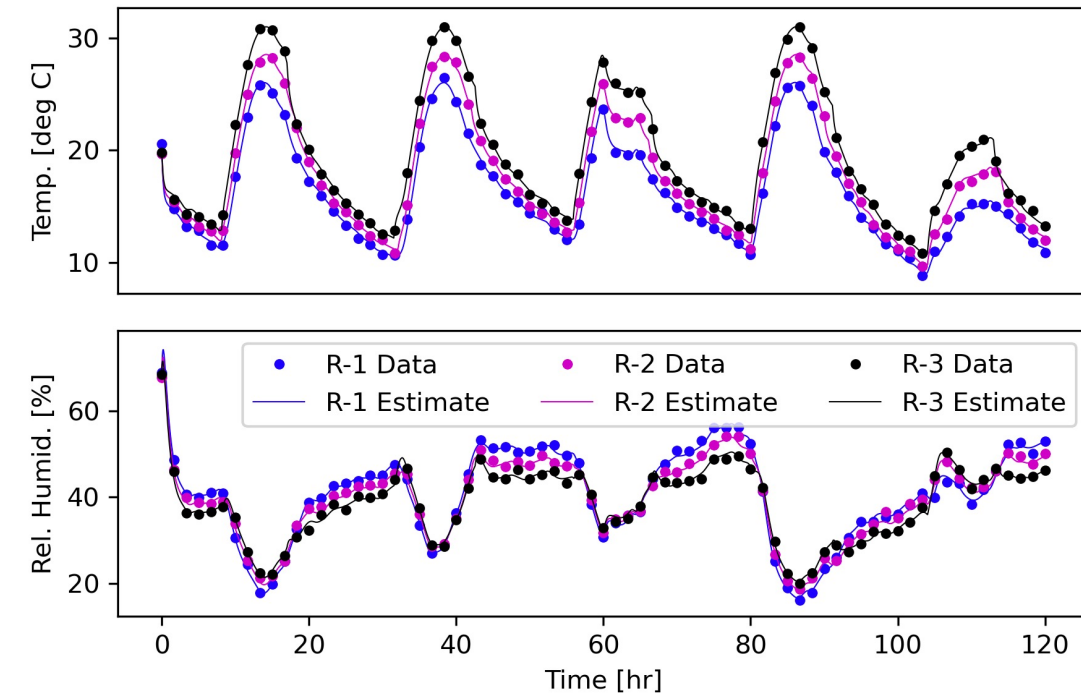


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ANP-BBO: Calibration Results

Measured and simulated outputs



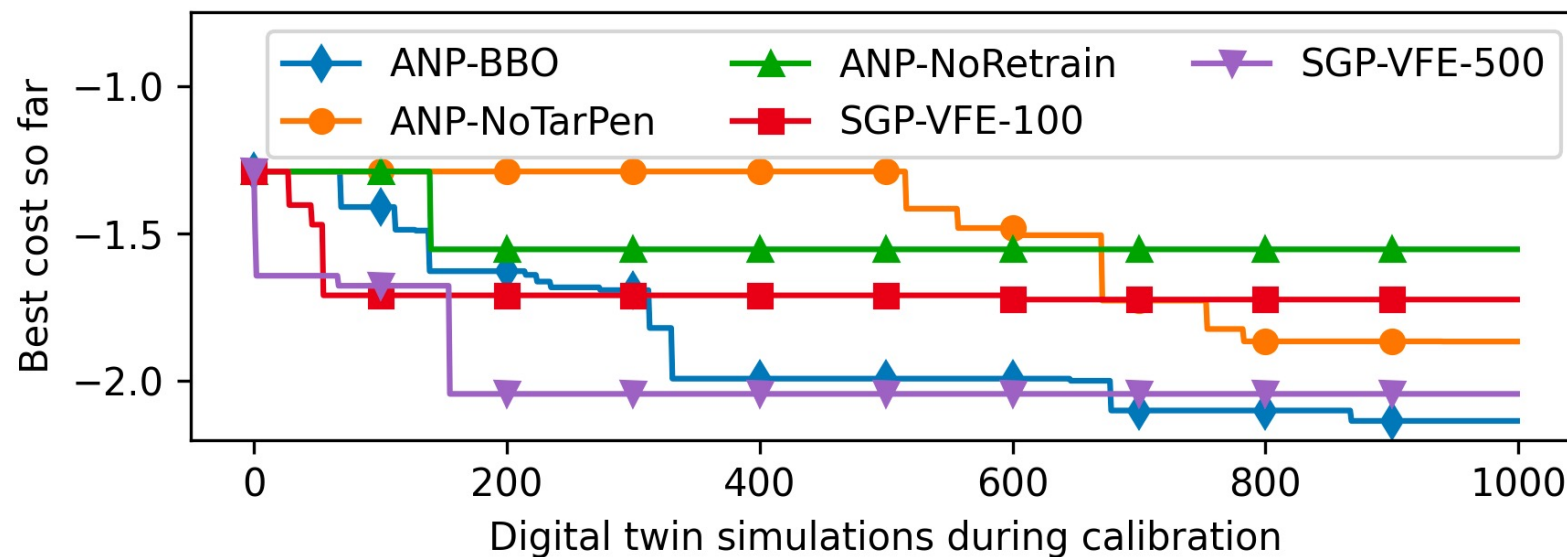
Outputs coefficient of variation of RMSE is **<1%**, well within the ASHRAE guidelines **<15%** ^[1]

[1] ASHRAE, *Guideline 14-2014, measurement of energy, demand, and water savings*. 2014.

R-x: Room number x, $x \in \{1,2,3\}$

ANP-BBO: Ablation Studies

1. *ANP-BBO*: Proposed algorithm
2. *ANP-NoTarPen*: Switch off target set penalization
3. *ANP-NoRetrain*: Train ANP once with initial data, no further retraining
4. *SGP-VFE-100/500*: Use sparse Gaussian processes^[1] as learner, with 100 or 500 inducing points



ANP-NoTarPen: Shows target penalization helps more than only latent sampling

ANP-NoRetrain: Lack of retraining with limited initial data does poorly

SGP-VFE: Good early, but gets stuck due to worsening approximations at scale

ANP-BBO: outperforms the others after 700 iters due to diverse and good candidates

[1] Titsias. *Variational learning of inducing variables in sparse Gaussian processes*. AISTATS, 2009.

